# EES: Efficient Data Structure for Decision Rules Evaluation in Evolutionary Learning\*

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Abstract. The increasing amount of information available is encouraging the search for efficient techniques to improve the data mining methods, especially those which consume great computational resources. We present a novel structure, called EES, which helps certain data mining algorithms which generate decision rules to reduce the aforementioned cost. It is of particular interest when the search for the solution involves a great many hypothetical solutions. Thus, this structure is designed for speeding up the rule-evaluation process in methods based on Evolutionary Algorithms. The traditional structure, based on vectors of examples (in which the database is stored) is evaluated and compared with EES, including the costs for a stratified set of cases. Finally, the experimental results demonstrate the quality of our proposal, reducing the computational cost by approximately 50%.

### 1 Introduction

Within the context of supervised learning there exist in the literature a large number of methods and algorithms that extract inherent knowledge from a labelled database and build a model which represents the extracted information. A great number of these methods (CN2 [2], RISE [4], OC1 [9], GABIL [3], GIL[7], etc) use probabilistic algorithms to look for solutions in space, with a high computational cost, principally due to the repetitive evaluation of the candidate solutions. This work focus on those systems that define a probabilistic heuristic for the generation of decision rules, especially on those methods that use an Evolutionary Algorithm (henceforth EA) in order to carry out such aim. Thus, we propose a data structure which reduces the computational cost of evaluation in the learning process.

The aforementioned methods usually evaluate the rules directly from the database. That is to explore such database sequentially, taking each of the examples and testing the quality of the rule through the correct classification of those examples. We can see, therefore, that the learning process of these systems is very costly in terms of time and space. Some authors [10, 11] have concentrated

<sup>\*</sup> This research was supported by the Spanish Research Agency CICYT under grant TIC2001-1143-C03-02.

their efforts on improving the learning process by speeding up the algorithm, in order to reduce its computational cost. Others have approached the problem from the perspective of scalability [12]. However, the appropriate organisation of the information could also contribute to the reduction of computing time. This aspect, no less important than the previous one, has perhaps been more neglected.

There are in the literature numerous proposals on data structures and organisation of the information which essentially speed up the search for information in multidimensional spaces, such as those known as Multidimensional Access Methods (MAM)[5]: Grid File , LSD-tree ,K-D-Tree , R-tree , etc. However, given the peculiarity of the problem we are facing, MAM do not, in themselves, provide a solution to such problem, since they index a dataset with the goal to speed up the queries on such data. However, we want to reduce the cost of evaluation of decision rules. To do it, we distributes the examples according to the values that they take for each attribute. Thus, we know exactly what examples fulfill these rules. For instance, AD-Tree [8] is the MAM that gives the nearest solution to the problem we want to solve. Nevertheless, if we would want to evaluate a decision rules using this structure, we would have to build the no sparse AD-Tree, that is to store all possible queries in addition to the indexes of the examples that each query includes. This means very high computational cost, since too mach redundant information is stored.

In this work we are presenting a data structure called EES (Efficient Evaluation Structure) which is designed specifically for accelerating the evaluation process of rules during the application of data mining algorithms based on EAs. The EES structure organises the information from a database in such a way that it is not necessary to process all the examples in order to evaluate decision rules generated by a supervised learning system.

An EA codifies decision rules as individuals in the genetic population. Once the population is constructed the individuals are evaluated and depending on the quality of each one of them, the crossover and mutation operators are applied, thus constructing the next generation. It is simple to see that those systems that apply EAs need to carry out constant evaluations throughout the learning process, since they have to evaluate each one of the individuals of each one of the populations that they generate. For example, an EA that carries out 300 generations, each containing 100 individuals, needs to carry out at least 30,000 evaluations. If the database contains 1000 examples the process will be carried out 30 million times. In the particular case of EAs applied to the generation of rules, the database is stored in a vector of examples (see Figure 1), which is used for evaluating of every individual. Evaluation by means of a linear search processes each and every one of the examples in the database independently of the conditions established by the rule. As can be seen in Figure 1, not all the covered examples are correctly classified (only Examples 4 and N).

Therefore the computational cost of a single evaluation is O(NM), where N is the number of examples and M is the number of attributes in the database. The rule-learning methods that EAs use invest approximately 85% of their time

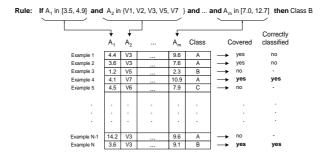


Fig. 1. Evaluation of a rule using a vector of examples.

in evaluating the individuals (the mean of the executions of a 10-fold cross-validation with 20 UCI Repository databases [1]). This is the reason why we propose the EES structure in order to organise the information in such a way that only the necessary examples from the database will be dealt with, and not all data.

## 2 Description

EES distributes the information from the database in such a way it is possible to carry out a search in the space by attribute instead of by example. The data structure must be capable of storing this information independent of the type of attribute (continuous or discrete). In the case of continuous attributes it is convenient to apply a method to transform them into discrete which reduces the cardinality of the set of values that this type of attributes can eventually take. In certain cases the methods of rule-generation apply a method of discretization as pre-processing of the data in order to calculate such intervals. EES must be constructed using the same sets of intervals obtained by the discretization method applied by the rule-generation method. This does not imply any kind of limitation as regards the data structure, since the latter is totally flexible as opposed to the discretization used by the continuous attributes. The only restriction demanded of the discretization method is that the generated intervals be disjoint, given that if this were not the case there could exist in the database a value pertaining to various intervals. In any case we will be able to maintain infinite rank, that is to say, we will not need to apply any discretization method. The EES structure would still be valid: in this case the number of nodes would increase and the size of the lists associated with the nodes would be reduced even to length equal to one.

In general, for every attribute  $A_i$  in the database we will denote the finite set of values that  $A_i$  can take by  $\Omega_i$ . In the case of  $A_i$  being a discrete attribute  $\Omega_i$  will contain values which we will represent as  $V_{ij}$   $(1 \le j \le |\Omega_i|)$ . On the other hand, if we are dealing with a continuous attribute,  $\Omega_i$  will contain intervals



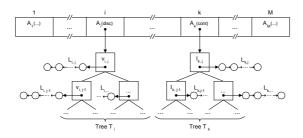


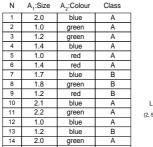
Fig. 2. General schema of EES.

which we will call  $I_{ij}$   $(1 \leq j \leq |\Omega_i|)$ , the lower and upper bounds of which we will denote by  $l_{ij}$  and  $u_{ij}$  respectively. In this manner EES will store the information of the continuous attributes in a similar way to that which it does for the discrete attributes: the lower and upper limits of each interval will be saved in place of the unique values that are stored for the discrete attributes.

EES arranges the information from the database in a vector of binary and balanced search-trees in such a way that the  $i^{th}$  element of the vector will contain information about the  $i^{th}$  attribute  $(A_i)$  in the database. Specifically, the different values or intervals that  $A_i$  can take are stored in the tree, which we will denote by  $T_i$ . In addition to  $V_{ij}$  or  $I_{ij}$ , each node  $N_{ij}$  of the tree  $T_i$  contains a list  $(L_{ij})$  of numbers which indicate the positions of examples in the database. If  $A_i$  is discrete, the indexes contained in the list  $L_{ij}$  will correspond to those examples, the  $i^{th}$  attributes of which take the  $j^{th}$  value  $(V_{ij})$  within the  $\Omega_i$  set of possible values of such attribute. If  $A_i$  is continuous, the indexes contained in  $L_{ij}$  will correspond to those examples, the value of which for the  $i^{th}$  attribute is included in the  $j^{th}$  interval  $(I_{ij})$  within the  $\Omega_i$  set of possible intervals of such attribute. Figure 2 shows the simplified general schema of the data structure for a database with M attributes, where the  $i^{th}$  attribute is discrete while the  $k^{th}$ is continuous. It is important to note that in the case of continuous attributes the tree is sorted (inorder) by (disjoint) intervals and in the case of discrete attributes it is arranged alphabetically by the discrete value. In this manner, any search within the tree has a logarithmic cost.

#### 2.1 Construction of the EES structure

Let us start from the information contained in a labelled database with N examples indexed from one to N, each of them with M attributes of any type (see Figure 3). In these M attributes we are not including the class. Previously a discretization method similar to the method 1R described by Holte in [6] has been applied, although any other supervised discretization method could have been used. This method obtains a set of disjoint intervals for each one of the continuous attributes in the database. For each attribute  $(A_i)$  a balanced searchtree is created and inserted in the structure in the corresponding position (i).



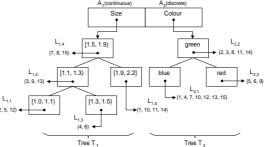


Fig. 3. Example.

The nodes of these trees contain the values or intervals according respectively to whether the attribute is discrete or continuous. Once all the trees have been created and inserted, the lists for each node are completed. A linear search of the database is carried out, passing through all the examples. For each attribute  $A_i$  of a specific example, the node corresponding to the value of such attribute will be searched for in the tree  $T_i$ . Once the node has been located, the index of the example being processed is inserted into the list of such node and the next attribute of this example is processed. When all the attributes of an example have been treated we say that the example has been inserted into the structure, and we go on to process the next example. At the point at which all the examples have been inserted, the structure contains the same information as the database, excepting the class of each example. However, this information is directly accessible during the use of the structure, since the latter stores the indexes of examples. The computational cost of the construction process of the data structure is  $O(NMlog_2|\overline{\Omega}|)$ , where  $\overline{\Omega}$  is the mean number of tree-nodes.

Figure 3 shows a labelled database with 15 examples (two attributes and two classes), and the EES structure that is obtained starting from the this database.

#### 2.2 Use of the EES

The fundamental property that the data structure offers is the possibility of accessing the information from the database through attributes instead of through examples. The main aim that we are looking for in the use of the data structure is not having to process those examples, the values of which are not covered by the rule which is being evaluated. If we take a node  $N_{ij}$  of each  $T_i$ , the intersection of the lists  $L_{ij}$  will be the set of the indexes of examples which fulfill that each one of its attributes  $A_i$  take values which are covered by each corresponding node  $N_{ij}$ . The advantage that the EES offers lies in the fact that the intersections are carried out in an incremental manner - that is to say, firstly the intersection of the list for the attribute  $A_1$  and the list for the attribute  $A_2$  is carried out. If

```
Function EVALUATE
   Inputs: R: Decision Rule; E: Data Structure
    Output: L: List of indexes (examples covered by R)
    L_i := ListUnion(R, E, i)
   while i < NumberOfAttributes(E) \land L_i \neq \emptyset

i := i + 1
      L_i := L_{i-1} \bigcap ListUnion(R, E, i)
   end while
    L := L_i
end EVALUATE
Function ListUnion
    Inputs: R: Decision Rule; E: Data Structure; k: Integer (attribute location)
    Output: Lu: List of indexes (examples covered by R.)
begin
    Lu := \emptyset; T_k := E[k];
   if A_k is Continuous
      for every I_{kj} \in T_k \mid I_{kj} \subseteq R_k
        Lu := Lu \bigcup L_{kj}
   end for else /* A_k is Discrete */ for every V_{kj} \in T_k \mid V_{kj} \in R_k
         Lu := Lu \bigcup L_{kj}
      end for
    end if
end ListUnion
```

Fig. 4. Algorithm for the use of EES.

such intersection is not empty, the list for the attribute  $A_3$  is searched for and a new intersection between this and the result of the previous intersection is created. This process is repeated until all the attributes are completed, or until one of the intersections remains empty. If the process concludes, the resulting list will contain the indexes of the examples which fulfill the values or intervals of all the selected nodes  $N_{ij}$ . If these nodes  $N_{ij}$  are searched for according to the conditions established by a decision rule, we will be evaluating such rule. The pseudo-code of the evaluation algorithm for decision rules using the EES is shown in Figure 4.

The notation used in the algorithm in Figure 4 is the same as that used in the general structure of Figure 2, excepting the following symbols: E represents the data structure and R is the rule to be evaluated, while  $R_i$  is the condition that R establishes for the attribute  $A_i$ . The symbol  $L_i$  (with a single subindex) represents the list of accumulated intersections until the  $i^{th}$  iteration, that is to say, until the  $i^{th}$  attribute. The algorithm is divided in two functions. The first, EVALUATE, is the main function and has as its input parameters the decision rule R and the data structure E. The rule R has the structure that is shown in Figure 1, the condition that R establishes for the  $k^{th}$  attribute in the database being represented by  $R_k$ . The function EVALUATE offers a single output parameter (L), which is the list of indexes of examples resulting from the evaluation of the rule R on the data structure E. In this way, the function EVALUATE searches the rule R and the structure E simultaneously, calculating

the intersections of the lists and returning the final list (L). The main function uses an auxiliary function named ListUnion, that has the rule R, the structure E and a integer which indicates the attribute which it has to deal with. The only output parameter of this function is the list of indexes (Lu) corresponding to the union of the lists  $L_{kj}$  for the attribute  $A_k$  (with  $1 \le j \le |\Omega_k|$ ). This union of lists is necessary owing to the fact that the condition of the rule R for the attribute  $A_k$  can include various nodes of the tree  $T_k$ . In the case of continuous attributes the first node included in the condition that the rule establishes is searched for in the tree. Once located, a inorder-walk of the tree starting from such node and stopping when it finds the first node which is not covered by the condition is carried out. In the case of discrete, it is necessary to search for all the values that the rule establishes for such attribute in the corresponding tree. When dealing with both cases of balanced search trees, all the searches carried out in them have a logarithmic cost.

## 3 Experiments

The experiments carried out to test the efficiency of the structure consist of evaluating various sets of decision rules for 15 different databases from the UCI Repository, as opposed to the linear search habitually used for the evaluation of decision rules. For each database groups of rules are generated in an aleatory manner, through use of a method which assures the uniform distribution of these rules. Subsequently, such rules are evaluated using the linear method and the data structure EES and the results obtained are compared.

The linear method of evaluation used in the tests is the most efficient one possible. For each rule this method searches the database, which has previously been stored in an vector of examples, processing each and every one of the examples. Likewise, for each example, the verification that its attributes fulfill the conditions of the rule is also carried out in a linear manner. However, it is not always necessary to process all the attributes of every example. If, during the processing of an example, one of its values does not fulfill the condition that the rule establishes for the corresponding attribute, that example is no longer processed as it will no longer be able to fulfill the rule, independent of the values that the rest of the attributes take, and the next example will be processed. Given that could think that the major advantage of the structure lies in the evaluation of rules which do not cover examples, in order to ensure that the test-method is fair two types of rules have been generated and evaluated: valid and invalid (see the results varying the percentage of valid rules in Figure 5). Let us call a rule valid if it covers at least one example in the database. In comparison, a rule which does not cover any of the examples in the database shall be called invalid. According to these definitions a valid rule will ensure that the structure is completely searched, while in the case of an invalid rule the evaluation process of the data structure will be halted before the search of the latter has been completed. Although, a priori, the evaluation of invalid rules seems to be pointless, this is not so, since the learning methods based on EA

BD	A.T. ESS	A.T. Vector	Improv.(%)
bupa liver disorder	1.464	4.370	66.5
breast cancer (Wisc.)	5.572	13.421	58.5
cars	2.173	4.870	55.4
cleveland	3.460	6.042	42.7
glass	1.634	2.884	43.3
hayes-roth	0.720	1.499	52.0
heart desease	3.018	6.228	51.5
iris	0.517	1.536	66.3
led7	20.689	34.905	40.7
letter	222.556	842.784	73.6
pima indian	4.283	11.309	62.1
soybean-	1.661	2.808	40.8
tic-tac-toe	7.623	11.031	30.9
vehicle	8.937	18.785	52.4
wine	2.084	4 120	49.4

Table 1. Comparison of average results and improvement.

generate intermediate rules which in many cases do not cover any examples. It is worth noting to take this into account, seeing that EES is focus on this kind of methods.

Table 1 shows the following: for each database (first column) the average time used by the EES structure (second column) and that used by the linear method (third column), as well as the improvement obtained by EES as compared with evaluation using the vector (final column). For each database the improvement is given by Equation 1, which represents the percentage of time saved by using the EES structure with respect to the time used by the vector in the average-case.

$$Improvement = 100 \times \frac{Time(Vector) - Time(EES)}{Time(Vector)}$$
 (1)

As can be observed in Table 1, for all the databases the average time taken by the EES is noticeably less than that taken by the vector. This ensures that the improvement will always be positive, that is to say, that the EES always improves on the linear structure. If we calculate the mean improvement for the 15 databases, we obtain the result that the average improvement is 52.4%, which is to say that the structure takes practically half as much time in evaluating the rules.

The experimental results are graphically shown in Figure 5. This Figure contains 15 graphs, one for each database used in the tests, which represent the evaluation time in seconds against the percentage of valid rules in the sets of rules evaluated. In turn, each graph contains two curves: the grey line shows the temporal results obtained for the evaluation using the vector of examples, while the black line refers to the results for the evaluation using the EES structure. Both representations show the temporal variation as the percentage of valid rules is increased. As graphs show, for all the databases used the behaviour of the EES structure is very favourable in comparison with the vector of examples. The first result that stands out is that for all the databases used, the evaluation time taken by the EES structure is inferior to the time spent by the linear method. The results show that EES is highly efficient independent of the type of rule (valid or invalid) which gives an idea of the robustness of the structure.

On the other hand, as the percentage of valid rules increases, so does the rule-evaluation time for both methods. In this sense, it is interesting that for 8 of the 15 databases (Figure 5: a, b, f, g, h, i, j, k) the approximate incline of the curve that represents the evaluation time for the method using EES is less pronounced than the incline for the linear method. This indicates that as the percentage of valid rules increases, the temporal evolution grows more slowly using the EES structure than using the vector of examples.

#### 4 Conclusions

In this work we are presenting the data structure called EES, the goal of which is to organise the information from a database in such a manner that the efficiency of the methods of generating decision rules based on Evolutionary Algorithms is improved. ESS allows us to process only those examples, the values of which are covered by such rule will be processed, and not the totality of the database. In this way, the evaluation process of examples is incremental, that is to say, it starts from a number of covered examples that is reduced as we analyse more attributes of the structure. When the number of covered examples is reduced to 0, the rule ceases to be of interest, and therefore is no longer evaluated. Thus EES calculates what examples are within a rule, if any; and not check if each example satisfies all the conditions of a rule, as the vector of examples would do. So this structure is not a method for indexing examples. Finally, the experimental results show the quality of our propose.

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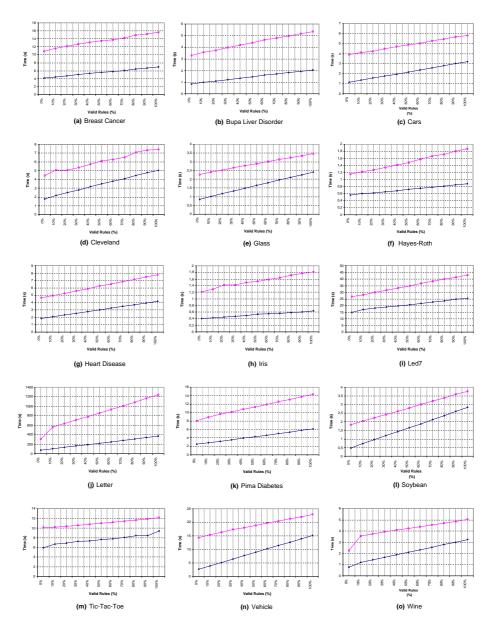


Fig. 5. Results.